



# Learning-based Current Estimation for DC/DC Converters Operating in Continuous and Discontinuous Conduction Modes

Gerardo Becerra, Fredy Ruiz, Diego Patino, Minh Tu Pham, Xuefang Lin-Shi



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Introduction

Problem Statement

Optimal Filtering for State Estimation of Unknown Systems

Results

Conclusion - Perspectives

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Problem Statement

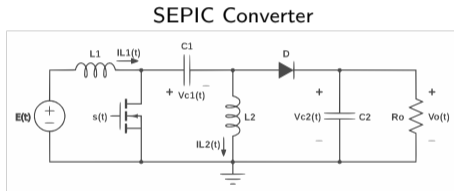
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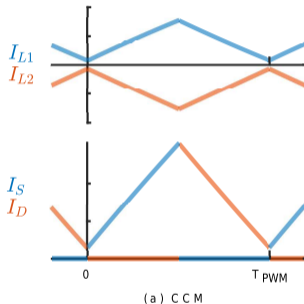
Conclusion - Perspectives

# Continuous/Discontinuous Conduction Modes (CCM/DCM)

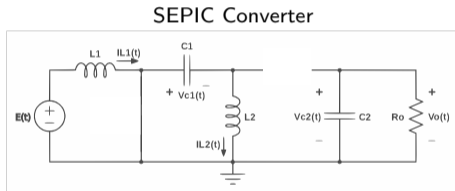
- ▶ PWM converters with two switches (e.g. MOSFET and diode).



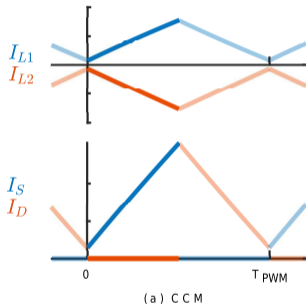
Continuous Conduction Mode



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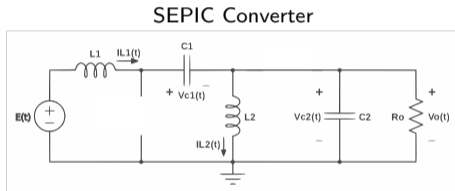


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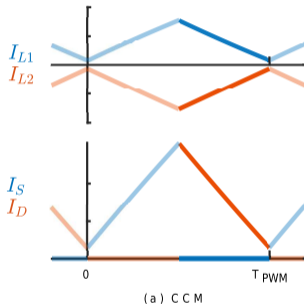


(a) CCM

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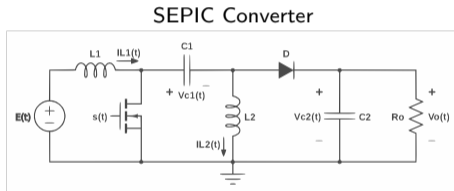
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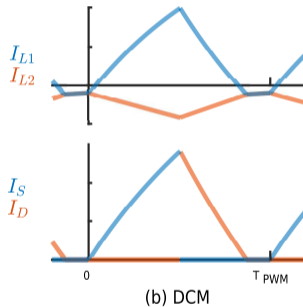
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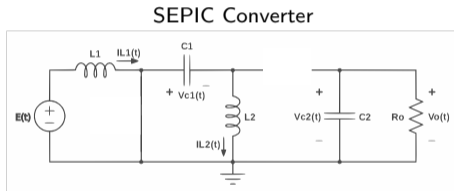


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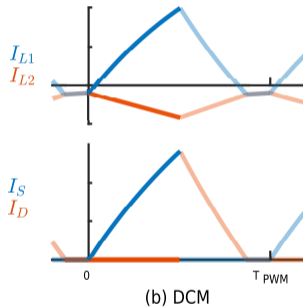


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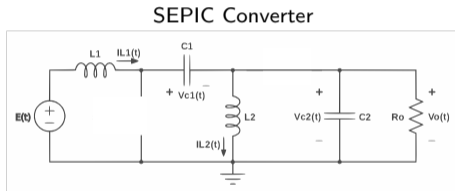


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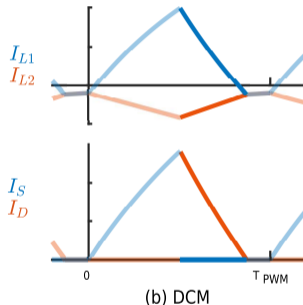


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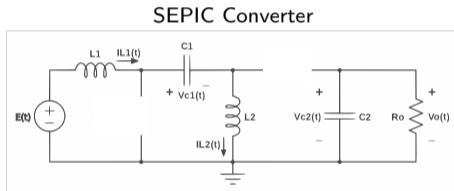


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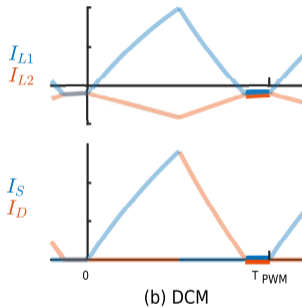


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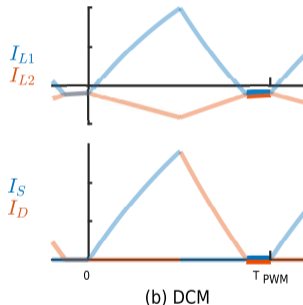
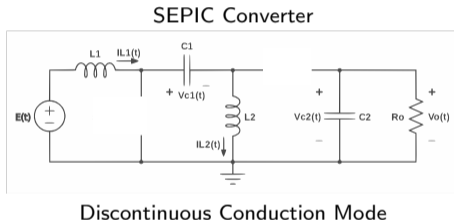


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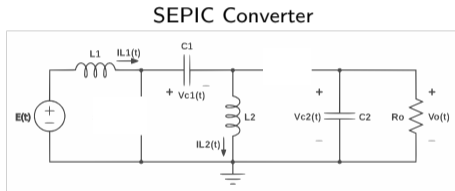
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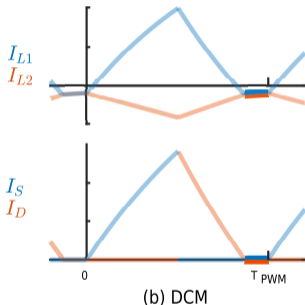


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Discontinuous Conduction Mode



- ▶ CCM-DCM transitions → change in dynamic properties.
- ▶ Hybrid behavior → complexity in observation problem.

- ▶ System of switched linear differential-algebraic equations.

$$\begin{aligned} \mathbf{P}_{\sigma(t)} \dot{\mathbf{x}}(t) &= \mathbf{A}_{\sigma(t)} \mathbf{x}(t) + \mathbf{B}_{\sigma(t)} \mathbf{u}(t) + \mathbf{B}_x w(t) \\ \mathbf{y}(t) &= \mathbf{C}_{\sigma(t)} \mathbf{x}(t) + \mathbf{D}_{\sigma(t)} \mathbf{u}(t) + \mathbf{B}_y w(t) \end{aligned} \quad (1)$$

- ▶  $\mathbf{x}(t) \in \mathbb{R}^{n_x}$ : state,  $\mathbf{u}(t) \in \mathbb{R}^{n_u}$ : input  $\mathbf{y}(t) \in \mathbb{R}^{n_y}$ : output.
- ▶  $\mathbf{B}_x w(t)$ : process noise ,  $\mathbf{B}_y w(t)$  measurement noise.
- ▶  $\mathbf{P}_{\sigma}$ ,  $\mathbf{A}_{\sigma}$ ,  $\mathbf{B}_{\sigma}$ ,  $\mathbf{C}_{\sigma}$ ,  $\mathbf{D}_{\sigma}$ : selected by the system mode  $\sigma(t) \in I$ .

- ▶ System matrices:

$$\mathbf{A}_{s(t),\delta(t)} = \begin{bmatrix} -R_{L1} - \beta R_{L2} & s - 1 & 0 & s\delta - \delta \\ 1 - s & s\delta & s - s\delta & s\delta \\ \beta & -s & \beta - R_{L2}(s + \delta - s\delta) & \delta - s\delta \\ \delta - s\delta & 0 & -\delta & -1/R_o \end{bmatrix},$$

$$\mathbf{B}_{s(t),\delta(t)} = \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \end{bmatrix}, \mathbf{P}_{s(t),\delta(t)} = \begin{bmatrix} L_1 & 0 & \beta L_1 & 0 \\ 0 & (1 - s\delta)C_1 & 0 & 0 \\ 0 & 0 & (s + \delta - s\delta)L_2 & 0 \\ 0 & s\delta C_1 & 0 & C_2 \end{bmatrix},$$

$$\mathbf{C}_{s(t),\delta(t)} = [0 \ 0 \ 0 \ 1], \mathbf{D}_{s(t),\delta(t)} = 0, \beta = (1 - s)(1 - \delta)$$

- ▶  $s(t)$ : Controlled switch state,  $\delta(t)$ : Uncontrolled switch state

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Consider the system in Eq. (1). Assume matrices  $\mathbf{P}_\sigma$ ,  $\mathbf{A}_\sigma$ ,  $\mathbf{B}_\sigma$ ,  $\mathbf{C}_\sigma$ ,  $\mathbf{D}_\sigma$ ,  $\mathbf{B}_x$ ,  $\mathbf{B}_y$  are unknown. Based on discrete-time measurements of  $\mathbf{u}$ ,  $\mathbf{y}$  and  $\mathbf{s}$ , obtain discrete-time estimates  $\hat{x}$  of the unmeasured state  $x$ .



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## Remarks:

- ▶ We assume no knowledge of the system model is available, but only measurements.
- ▶ We assume hybrid behavior (CCM & DCM operation) might be present in the system.

- ▶ Data-based estimation for PWM power converters in a wide operation range (CCM-DCM).

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- ▶ Use of principal component analysis (PCA) for dimensionality reduction of the datasets.

Discrete-time nonlinear system

$$\begin{aligned}\mathbf{x}_{k+1} &= \mathbf{F}(\mathbf{x}_k, \mathbf{u}_k, \mathbf{d}_k, w_k) \\ \mathbf{y}_k &= \mathbf{G}(\mathbf{x}_k, \mathbf{u}_k, \mathbf{d}_k, w_k)\end{aligned}$$

Causal estimator for state variable

$$v_k = x_{i,k}, i \in [1, \dots, n_x]:$$

$$\begin{aligned}\hat{v}_k &= f(\tilde{\mathbf{d}}_k, \tilde{\mathbf{y}}_k, \tilde{\mathbf{u}}_k, \tilde{\mathbf{d}}_{k-1}, \tilde{\mathbf{y}}_{k-1}, \tilde{\mathbf{u}}_{k-1}, \\ &\dots, \tilde{\mathbf{d}}_{k-m+1}, \tilde{\mathbf{y}}_{k-m+1}, \tilde{\mathbf{u}}_{k-m+1}).\end{aligned}$$

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- ▶ **Approach:** Set Membership framework for system identification [4].

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Assume dataset of measurements  $\mathcal{D} = \{(\tilde{\varphi}_i, \tilde{v}_i), i = 1, 2, \dots, N\}$  is available.

Prior assumptions on  $f_0$ :

$$f_0 \in \mathcal{F}(\gamma) := \left\{ f \in C^1 : \|f'(\varphi)\| \leq \gamma, \forall \varphi \in \mathbb{R}^{(n_d+n_y+n_u)m} \right\}$$

Prior assumptions on noise:

$$W \in \mathcal{W} = \{[w_1, w_2, \dots, w_T] : |w_k| \leq \varepsilon, \forall k=1, 2, \dots, T\}$$

Define the feasible filter set (FFS):

$$FFS \doteq \{f \in \mathcal{F}(\gamma) : |\tilde{v}_i - f(\tilde{\varphi}_i)| \leq \varepsilon, i = 1, \dots, N\}$$

## Theorem

1. A necessary condition for the FFS to be non-empty is:

$$\bar{f}(\tilde{\varphi}_i) \geq \tilde{v}_i - \varepsilon, \quad i = 1, \dots, N$$

2. A sufficient condition for the FFS to be non-empty is:

$$\bar{f}(\tilde{\varphi}_i) > \tilde{v}_i - \varepsilon, \quad i = 1, \dots, N$$

The worst-case bounds are defined as:

$$\bar{f}_c(\tilde{\varphi}_k) = \min_{i=1,\dots,N} (\tilde{v}_i + \varepsilon + \gamma \|\tilde{\varphi}_k - \tilde{\varphi}_i\|)$$

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The **direct filter (DF)** is defined as:

$$\hat{x}_k = f_c(\tilde{\varphi}_k) = \frac{1}{2} [\bar{f}(\tilde{\varphi}_k) + \underline{f}(\tilde{\varphi}_k)]$$

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## Algorithm 1: Direct Filter learning for power converters (offline)

---

**Result:**  $\mathcal{D}, \gamma, \varepsilon$

1. Design random test signals  $\tilde{\mathbf{d}}(t), \tilde{\mathbf{u}}(t)$  for driving the power converter to operate under varied conditions (CCM and DCM)
  2. Measure  $\tilde{\mathbf{y}}(t), \tilde{\mathbf{v}}(t)$
  3.  $\bar{\mathbf{y}}(t) = \text{average}(\tilde{\mathbf{y}}), \bar{\mathbf{v}}(t) = \text{average}(\tilde{\mathbf{v}}), \text{average}(\cdot) := \text{non-causal filter}$
  4.  $\tilde{\mathbf{y}}_k = \text{resample}(\bar{\mathbf{y}}(t), T_s), \tilde{\mathbf{v}}_k = \text{resample}(\bar{\mathbf{v}}(t), T_s), \tilde{\mathbf{d}}_k = \text{resample}(\tilde{\mathbf{d}}(t), T_s), \tilde{\mathbf{u}}_k = \text{resample}(\tilde{\mathbf{u}}(t), T_s),$
  5. Prepare dataset  $\mathcal{D} = \{\tilde{\varphi}_i, \tilde{\mathbf{v}}_i, i = 1, 2, \dots, N\}$  using  $\tilde{\mathbf{d}}_k, \tilde{\mathbf{y}}_k, \tilde{\mathbf{u}}_k, \tilde{\mathbf{v}}_k$
  6. Take  $\varepsilon = \|\tilde{\mathbf{v}}(t) - \bar{\mathbf{v}}(t)\|_\infty$
  7. Take  $\gamma^* = \min \gamma$ , subject to  $\bar{f}(\tilde{\varphi}_i) > \tilde{\mathbf{v}}_i - \varepsilon, i = 1, \dots, N$  (sufficient condition in Theorem 1 [5])
-

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**Algorithm 2:** Direct filtering estimation for power converters (online)

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**Data:**  $\mathcal{D}, \gamma, \varepsilon$

**Result:**  $\hat{v}_k$

**while true do**

1. Measure  $\tilde{d}_k, \tilde{y}_k, \tilde{u}_k$
2.  $\tilde{\varphi}_k = [\tilde{\mathbf{d}}_k^m; \tilde{\mathbf{y}}_k^m; \tilde{\mathbf{u}}_k^m]$
3.  $\bar{f}(\tilde{\varphi}_k) = \min_{i=1, \dots, N} (\tilde{v}_i + \varepsilon + \gamma \|\tilde{\varphi}_k - \tilde{\varphi}_i\|)$   
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4.  $\hat{v}_k = f_c(\tilde{\varphi}_k) = \frac{1}{2} [\bar{f}(\tilde{\varphi}_k) + \underline{f}(\tilde{\varphi}_k)]$

**end**

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- ▶ Provides a measure of uncertainty of the estimation.
- ▶ Finite Impulse Response (FIR) structure: BIBO stable.

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Kernel 1 :  $\psi_i^j = (\tilde{\varphi}_k^j - \tilde{\varphi}_i^j)^2, i = 1, \dots, N \quad j = 1, \dots, 3m.$

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Kernel 2 :  $\Delta_i = \sqrt{\sum_{j=1}^{3m} \psi_i^j}, \bar{f}_i = \tilde{v}_i + \varepsilon + \gamma \Delta_i, \underline{f}_i = \tilde{v}_i - \varepsilon - \gamma \Delta_i.$

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Kernel 3 :  $\bar{f} = \min_{i=1, \dots, N}(\bar{f}_i), \underline{f} = \max_{i=1, \dots, N}(\underline{f}_i).$

- ▶ **Contribution:** Principal component analysis (PCA) on regressor dataset to improve computation performance.

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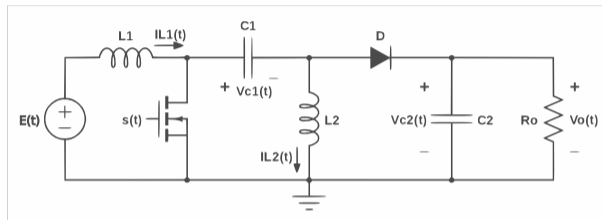
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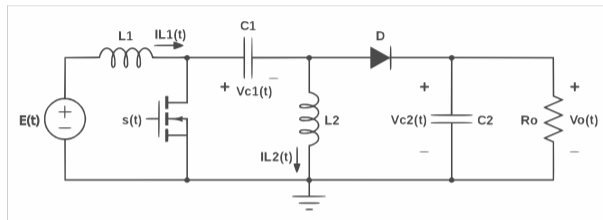
# Example: SEPIC Converter



**Observation problem:** Compute estimates of current  $I_{L1}(t)$  from measurements of input voltage  $E(t)$ , output voltage  $V_o(t)$  and duty cycle  $d(t)$  in PWM input  $s(t)$  for the SEPIC converter operating in both CCM and DCM.



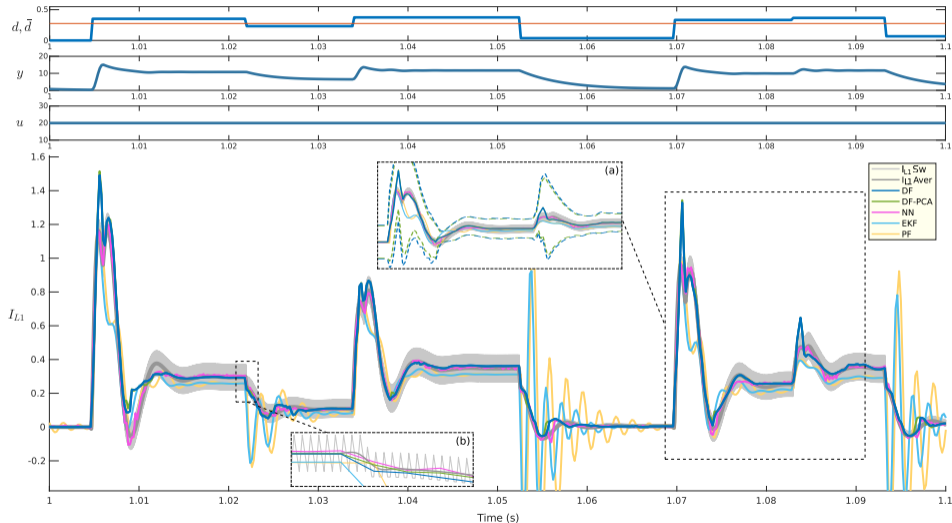
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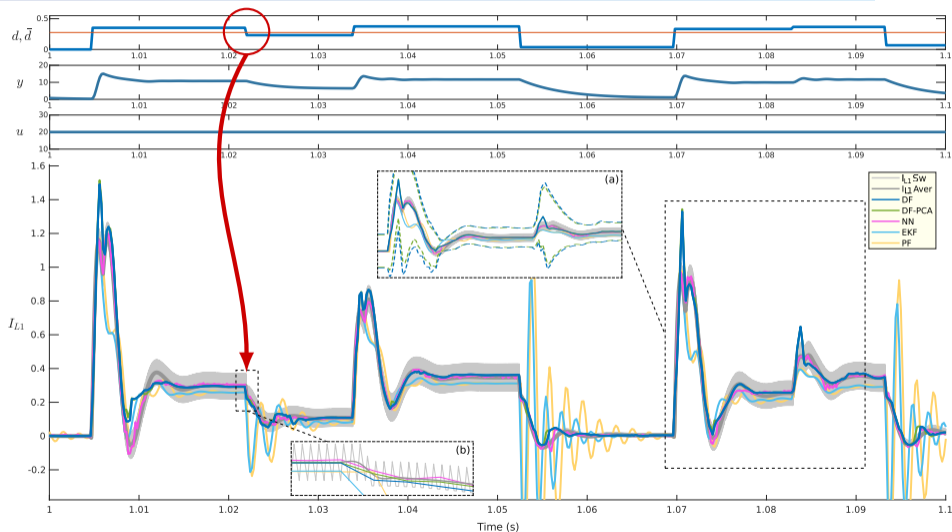
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Comparison of direct filter (DF), direct filter with PCA-reduced dataset (DF+PCA), neural networks (NN), extended Kalman Filter (EKF) and particle filter (PF).

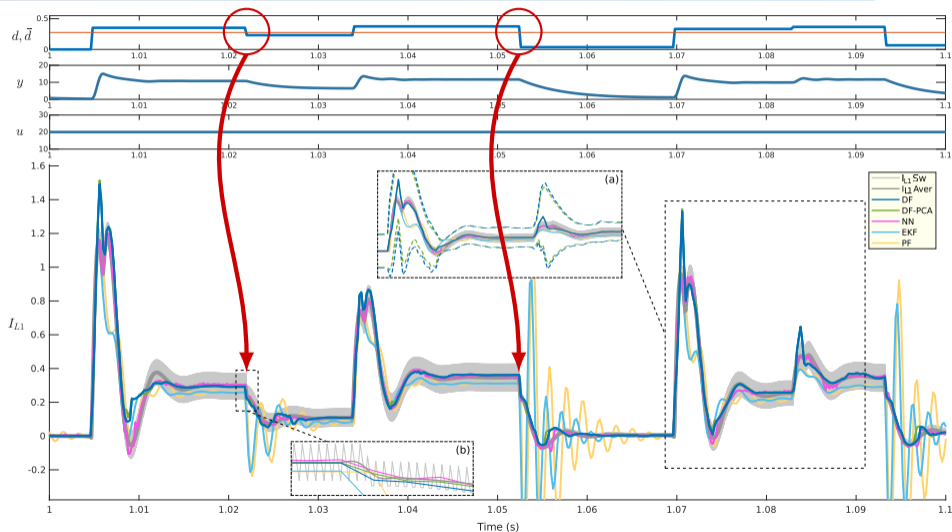
# Example: SEPIC Converter - Simulation Results



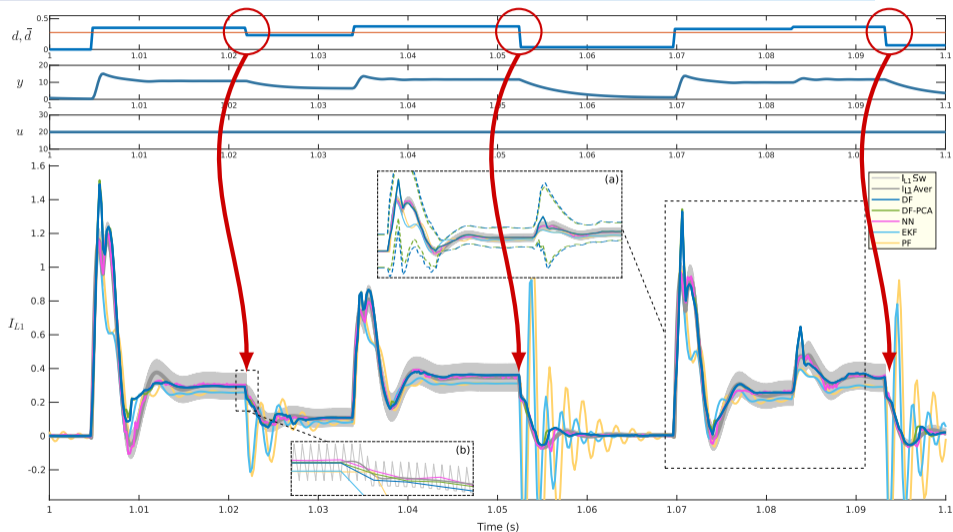
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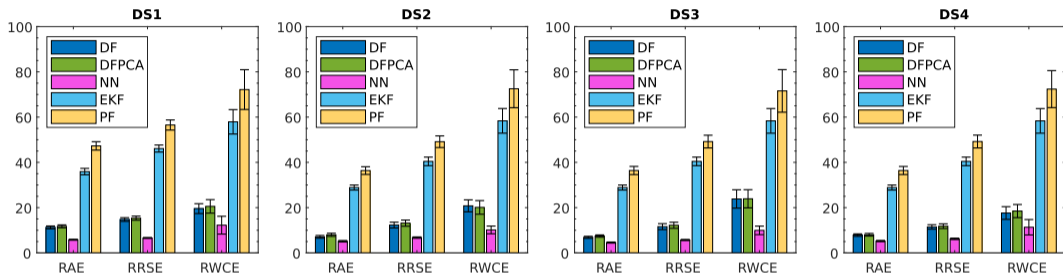
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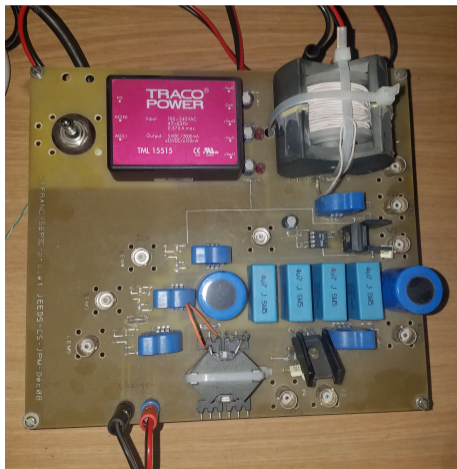
## Performance measures:

Relative absolute error:  $RAE = 100 \|\mathbf{v} - \hat{\mathbf{v}}\|_1 / \|\mathbf{v} - \bar{\mathbf{v}}\|_1$

Root relative square error:  $RRSE = 100 \|\mathbf{v} - \hat{\mathbf{v}}\|_2 / \|\mathbf{v} - \bar{\mathbf{v}}\|_2$

Worst-case error:  $RWCE = 100 \|\mathbf{v} - \hat{\mathbf{v}}\|_\infty / \|\mathbf{v} - \bar{\mathbf{v}}\|_\infty$

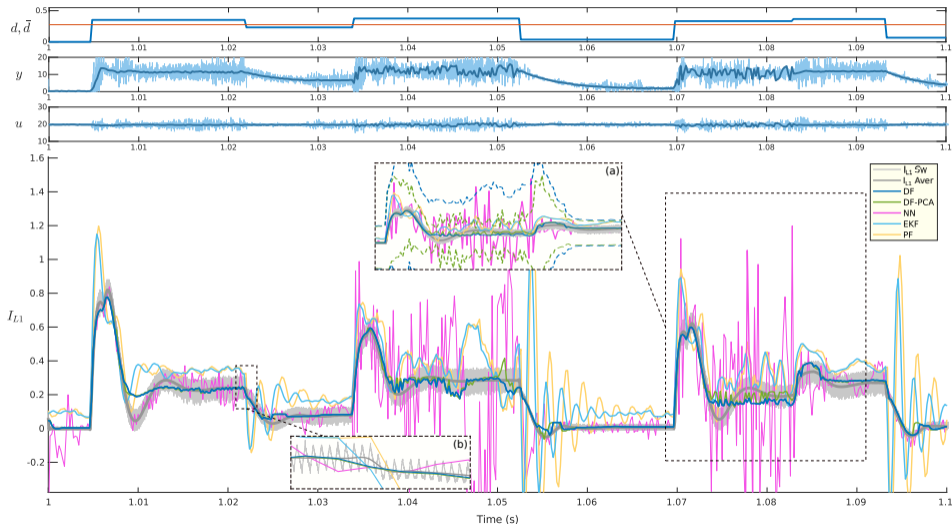
# Example: SEPIC Converter - Experimental Results



Converter	Parameters
SEPIC	$u(t) = 20 \text{ V}$ , $L_1 = 2.3 \text{ mH}$ , $C_1 = 190 \mu\text{F}$ , $L_2 = 330 \mu\text{H}$ , $C_2 = 190 \mu\text{F}$ , $R_{L1} = 2.134 \Omega$ , $R_{L2} = 0.234 \Omega$ , $R_o = 22 \Omega$ .

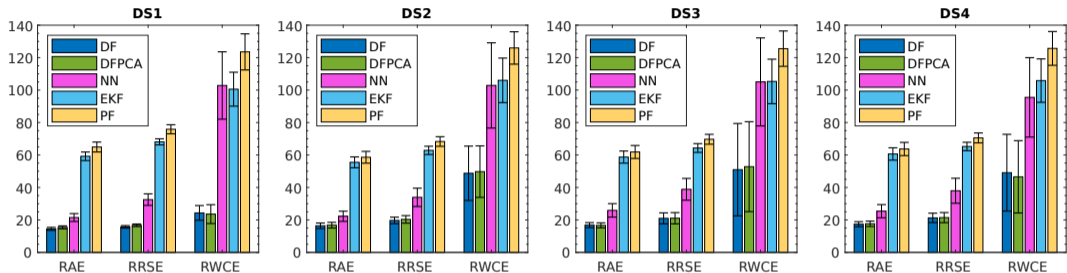
SEPIC converter test bench available at Laboratoire Ampère

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Dataset	Mean performance loss (%)			Execution time (ms) / speedup w.r.t CPU		
	RAE	RRSE	RWCE	CPU	GPU	GPU+PCA
DS1	1.5446	1.6832	3.0170	1.6410	1.0141 / 1.6183X	0.2419 / 6.7847X
DS2	0.2641	0.8726	4.0489	1.6445	1.0157 / 1.6191X	0.2434 / 6.7577X
DS3	0.6703	0.1592	6.4868	1.6491	1.0172 / 1.6212X	0.2437 / 6.7660X
DS4	0.4993	0.7582	1.9521	1.6428	1.0176 / 1.6144X	0.2443 / 6.7235X

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Performance loss is small compared to gains in computation speed!

Introduction

Problem Statement

Optimal Filtering for State Estimation of Unknown Systems

Results

Conclusion - Perspectives

**With respect to the state-of-the-art, we have introduced:**

- ▶ A **practical approach** to direct filtering in power converters using **parallel programming** and **data compression**.

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- ▶ A **practical approach** to direct filtering in power converters using **parallel programming** and **data compression**.
- ▶ An estimation approach that works on a **wide operation range**, without requiring a **complex system model**.

- ▶ Implementation in an RTOS platform where GPU kernel execution can satisfy deterministic constraints.

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- ▶ Implementation in an RTOS platform where GPU kernel execution can satisfy deterministic constraints.
- ▶ Investigate **dependence of estimation performance on parameters  $m$ ,  $N$**  for different converter topologies.
- ▶ Investigate **relation between performance loss and dimension of PCA transformation**.
- ▶ Investigate **other dimensionality reduction approaches** (Kernel PCA, linear discriminant analysis, generalized discriminant analysis, auto-encoders).

Thank you for your attention.

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Consider the following discrete-time linear system. Assume it is n-step observable.

$$\begin{aligned}x^{t+1} &= A(\tilde{d}^t)x^t + B_u(\tilde{d}^t)\tilde{u}^t + B_w(\tilde{d}^t)w^t \\ \tilde{y}^t &= C(\tilde{d}^t)x^t + D_u(\tilde{d}^t)\tilde{u}^t + D_w(\tilde{d}^t)w^t\end{aligned}$$

### Definition (n-step Observability)

$(A(\tilde{d}^t), C(\tilde{d}^t))$  is n-step observable if, for any time  $t$  and any sequence  $\tilde{d}^t$ , the state  $x^t$  can be uniquely determined by the corresponding zero-input response  $y^t$  for  $k = t, \dots, t + n - 1$ .

n-step observability matrix of the system:

$$O_k^n = \begin{bmatrix} C^{t+n-1}\Phi^{t+n-1,t} \\ \vdots \\ C^{t+1}\Phi^{t+1,t} \\ C^t \end{bmatrix}$$

Transition matrix of the system:

$$\Phi^{t_2,t_1} = \begin{cases} A^{t_2-1}A^{t_2-2} \dots A^{t_1}, & t_2 > t_1 \\ I, & t_2 = t_1 \end{cases}$$

- ▶ Since the system is assumed to be  $n$ -step observable, it follows that  $\text{rank}(\mathcal{O}_n^t) = n$ . Therefore, the inverse of  $\mathcal{O}_n^t$  exists.
- ▶ In practice: Run the estimator assuming  $(A(\tilde{d}^t), C(\tilde{d}^t))$  are known, and find minimum  $n$  such that  $\text{rank}(\mathcal{O}_n^t) = n$ .
- ▶ SEPIC converter in CCM:  $n = 20$ .

Evolution of  $\tilde{y}$  from  $t - n$  to  $t - 1$ :

$$\mathbf{y}^{t-1,n} = \mathcal{O}_n^{t-n} \mathbf{x}^{t-n} + \mathcal{T}_u^{t-n,n} \mathbf{u}^{t-1,n} + \mathcal{T}_w^{t-n,n} \mathbf{w}^{t-1,n}$$

$$\mathcal{T}_\alpha^{t-1,n} = \begin{bmatrix} D_\alpha^{t-1} & C^{t-1} \Phi^{t-1,t-1} B_\alpha^{t-2} & C^{t-1} \Phi^{t-1,t-2} B_\alpha^{t-3} & \dots & C^{t-1} \Phi^{t-1,t-n+1} B_\alpha^{t-n} \\ \mathbf{0} & D_\alpha^{t-2} & C^{t-2} \Phi^{t-2,t-2} B_\alpha^{t-3} & \dots & C^{t-2} \Phi^{t-2,t-n+1} B_\alpha^{t-n} \\ \mathbf{0} & \mathbf{0} & D_\alpha^{t-3} & \dots & C^{t-3} \Phi^{t-3,t-n+1} B_\alpha^{t-n} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ \mathbf{0} & \mathbf{0} & \mathbf{0} & \ddots & D_\alpha^{t-n} \end{bmatrix}$$

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